

Investigation of the effect of wind uncertainty/fluctuation on wake vortex transport NGE/IGE

N. Bourgeois, I. De Visscher, G. Winckelmans and L. Bricteux

Université catholique de Louvain (UCL)

Louvain School of Engineering (EPL)

Institute of Mechanics, Materials and Civil Engineering (iMMC)

1348 Louvain-la-Neuve, Belgium

WakeNet3-Europe Workshop

Short-Term Weather Forecasting for Probabilistic Wake-Vortex Prediction

Institut für Physik der Atmosphäre, DLR Oberpfaffenhofen

10/11 May 2010

Overview of the presentation

Introduction

1. Influence on the WV transport of the distribution of V_{10} [m/s] (crosswind speed at an altitude of 10m)
2. Influence on the WV transport of the distributions of both V_{10} [m/s] and the aircraft altitude h_0 [m]
3. Influence on the WV transport of the distribution of the orientation of the crosswind α [$-$]

Introduction

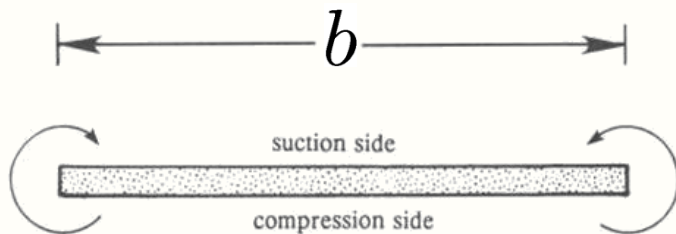
Aircraft wake vortices

$$L = \rho U_{\infty} b_0 \Gamma_0 = M g$$

$$\Gamma_0 = \frac{M g}{\rho U_{\infty} b_0} \quad \text{circulation}$$

$$V_0 = \frac{\Gamma_0}{2\pi b_0} \quad \text{sink velocity}$$

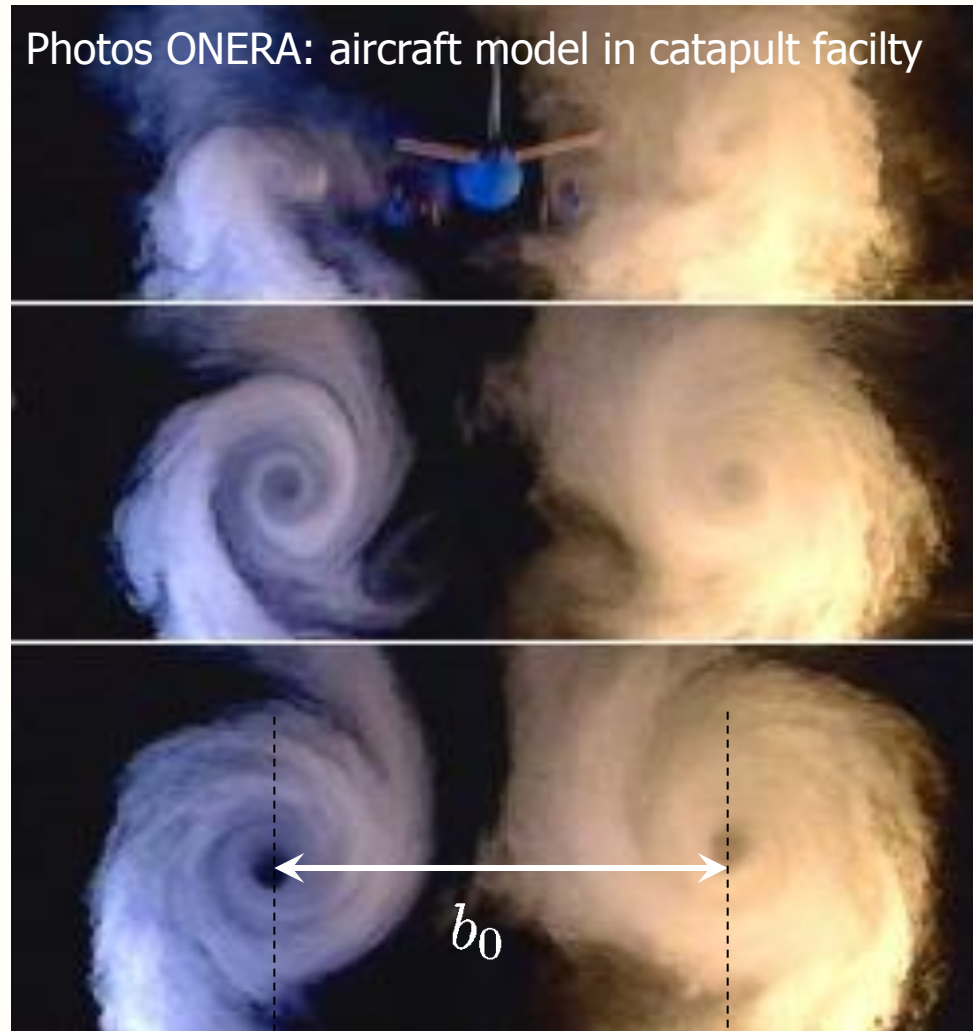
$$t_0 = \frac{b_0}{V_0} \quad \text{reference time}$$



$$b_0 = 0.72 \dots 0.84 b$$

depending on a/c and on wing configuration

Photos ONERA: aircraft model in catapult facility





Introduction

Operational modeling of WV behavior (transport and decay)

The Deterministic wake Vortex Model (DVM) is a wake vortex predictor software developed by UCL.

It integrates, in time, various physical models so as to forecast, in real-time, the transport and decay of the wake vortices in one computational gate (i.e., one slice of space along the flight path).

It includes models of:

- time-to-demise evaluation (with EDR and stratification effects)
- two-phase decay (choice between two EDR-based models and one TKE-based model)
- near-ground effects (NGE)
- in-ground effects (IGE)
- wind shear effects
- stratification effects

It takes, as inputs:

- the aircraft characteristics (altitude, weight, TAS, span and wing loading factor)
- the met. conditions: wind (cross and head), turbulence and stratification profiles



Introduction

Operational modeling of WV behavior (cont.)

Probabilistic modeling and assessment of WV is what is operationally required.

The Probabilistic wake vortex model (PVM) is an upper software layer that is based on a Monte-Carlo approach, using the DVM as a subtool.

For each PVM run, many deterministic runs are performed, with variations on the impact parameters:

- met. conditions,
- a/c characteristics,
- coefficients of the physical models

An operationally usable statistical analysis (PDF, mean, variance, confidence envelopes) is then obtained from the results.

(1) Influence of V_{10} [m/s] distribution

- Classical logarithmic profile: $\frac{V(z)}{V_\tau} = \frac{1}{\kappa} \log \left(\frac{z + z_0}{z_0} \right)$,

with $\kappa = 0.40$ [—] the von Karman constant,

z_0 the roughness height (typically $z_0 = 0.01$ [m] for short grass) and

V_τ the friction speed (determined by $V_{10} = V(z = 10)$)

- Two investigated distributions: uniform and normal
- Identical μ and σ for both distributions
- Uniform distribution:

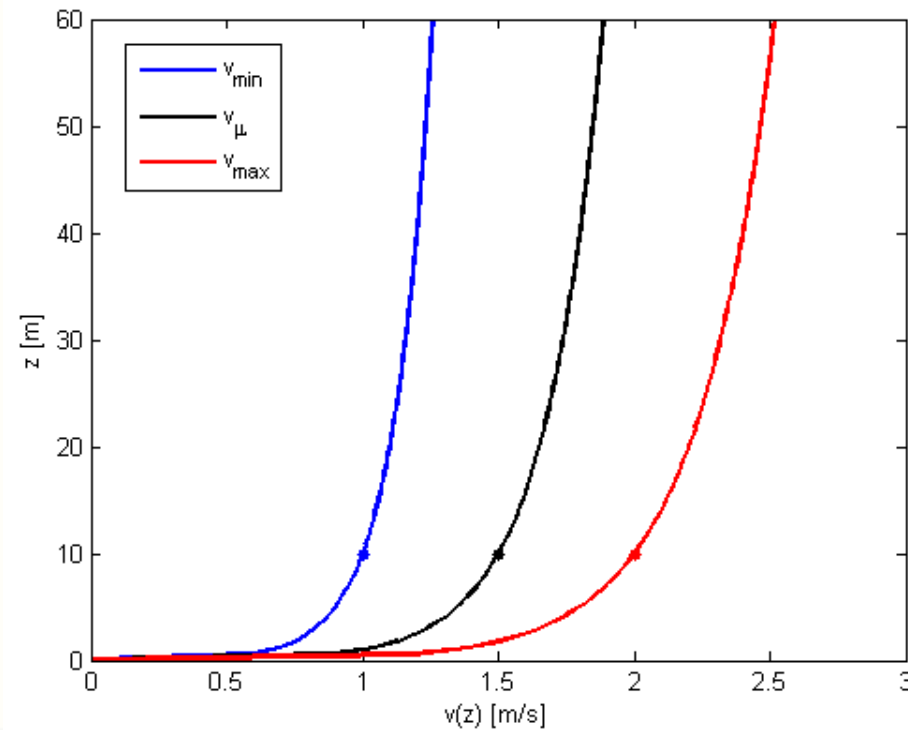
$$V_{10_{\min}} = 1.00 \text{ [m/s]}$$

$$V_{10_{\max}} = 2.00 \text{ [m/s]}$$

- Normal distribution:

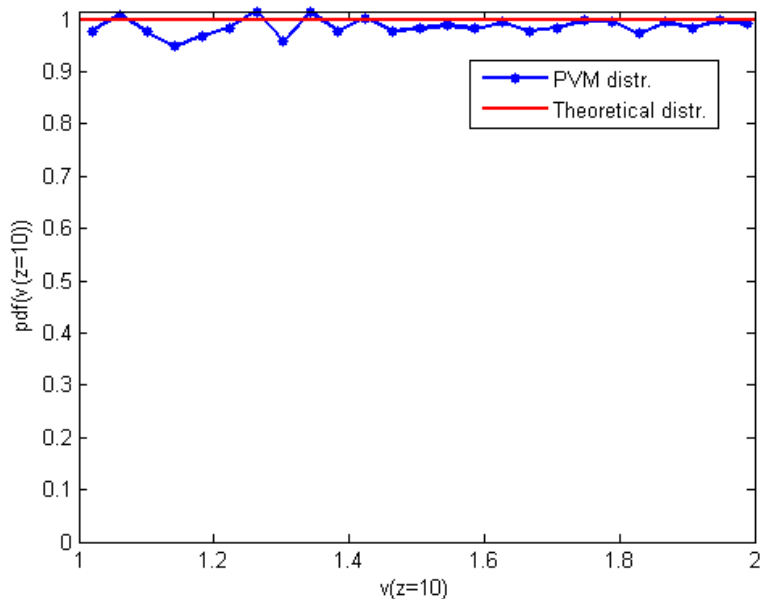
$$\mu(V_{10}) = 1.50 \text{ [m/s]}$$

$$\sigma(V_{10}) = 0.29 \text{ [m/s]}$$

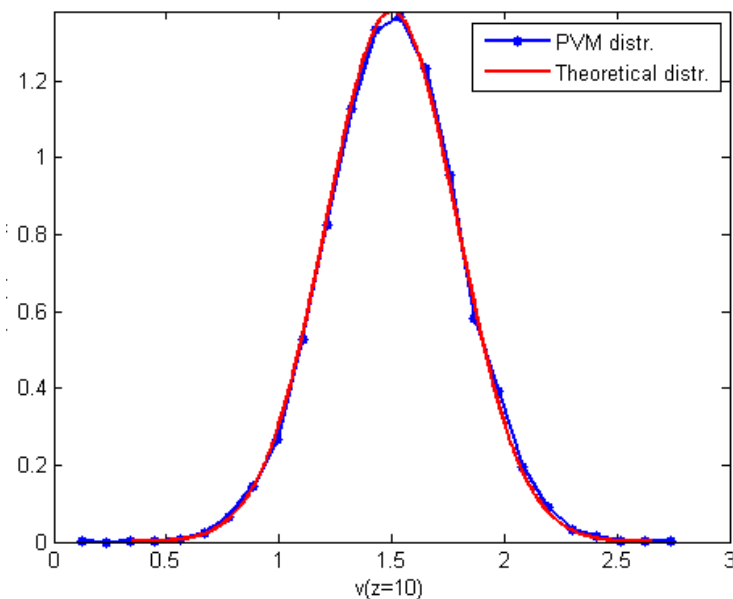


(1) Influence of V_{10} [m/s] distribution

- Studied case (IGE) : $b = 60.3$ [m], $M = 180\,000$ [kg], $s = b_0/b = 0.75$ [$-$],
 $h_0 = 40.0$ [m], $TAS = 70.0$ [m/s]
- Everything is deterministic, apart from the crosswind
- PVM simulations: 100 000 runs for each distribution
- Discrete inputs PDF obtained by random picking in the continuous PDF:



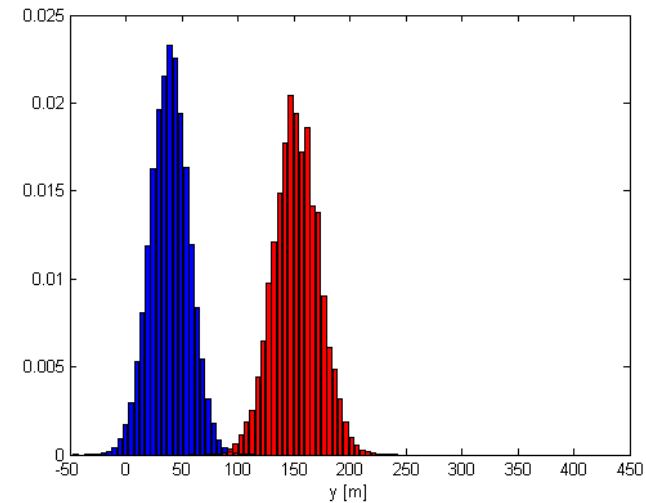
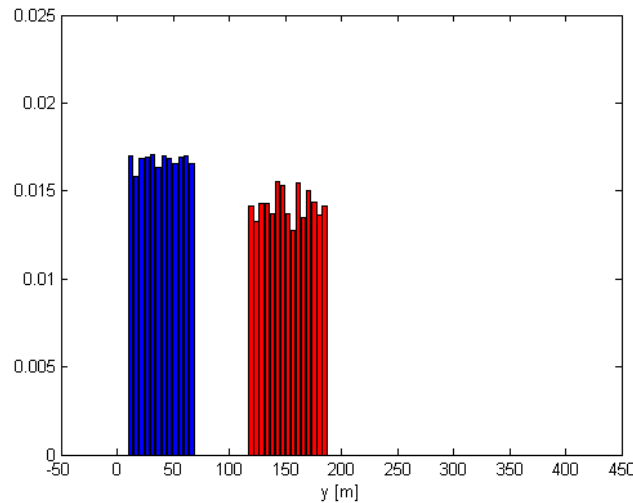
Uniform distribution



Normal distribution

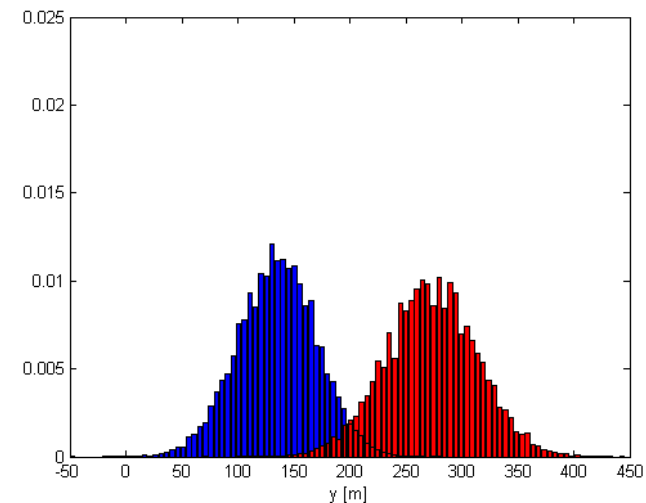
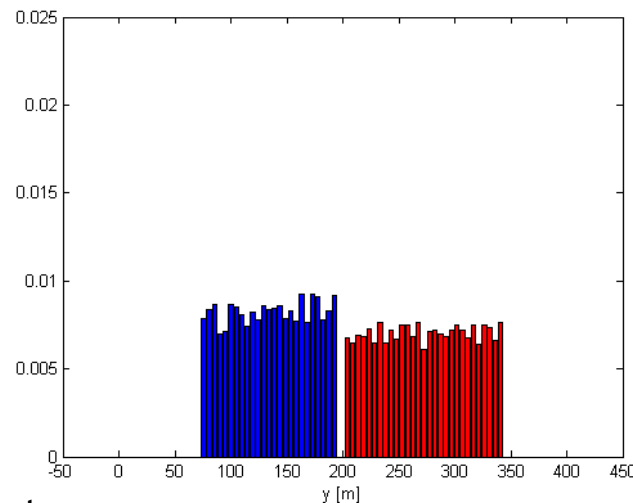
Effect on the lateral position of the vortices: discrete PDF

- After $t = 60$ [s] (left/right : uniform/normal distribution of V_{10}) :



Bin size =
5m

- After $t = 120$ [s] :

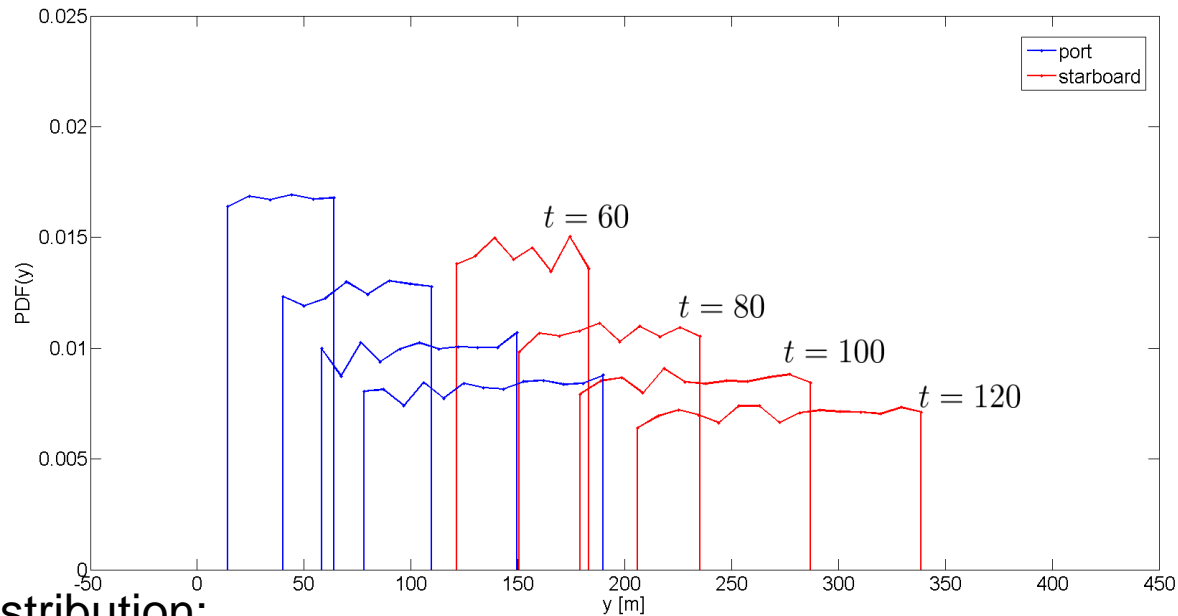


Blue: port vortex

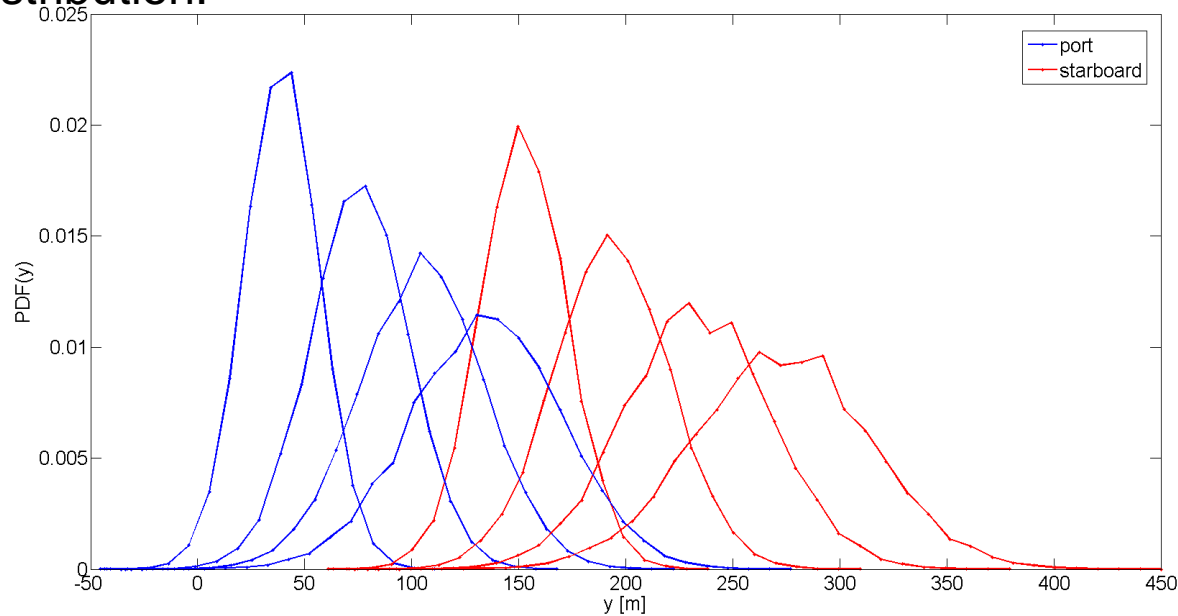
Red: starboard vortex

Evolution of the lateral position discrete PDF

- Uniform distribution:

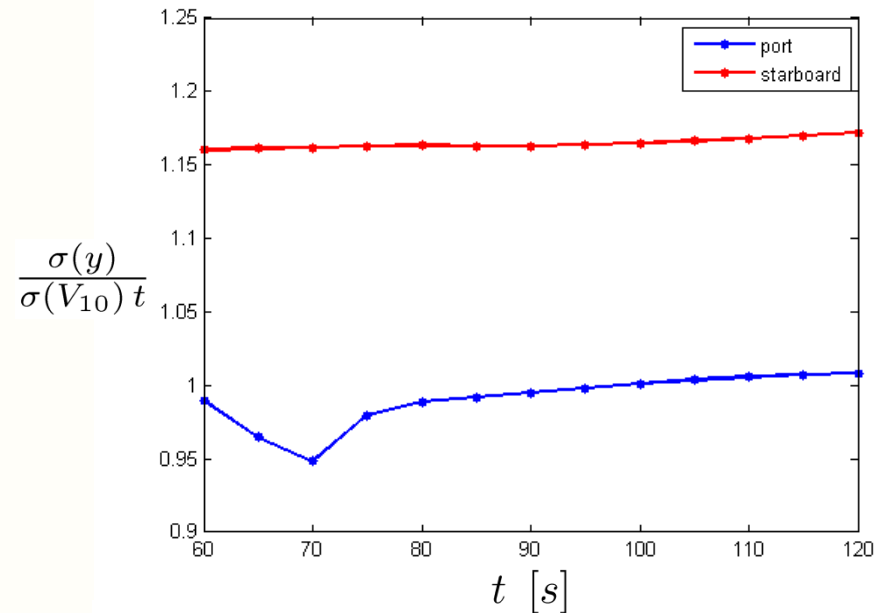
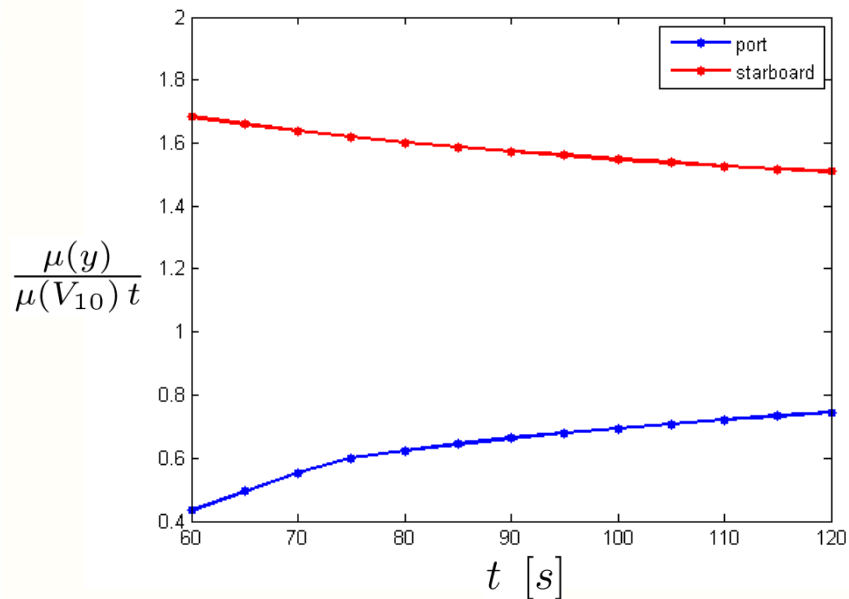


- Normal distribution:

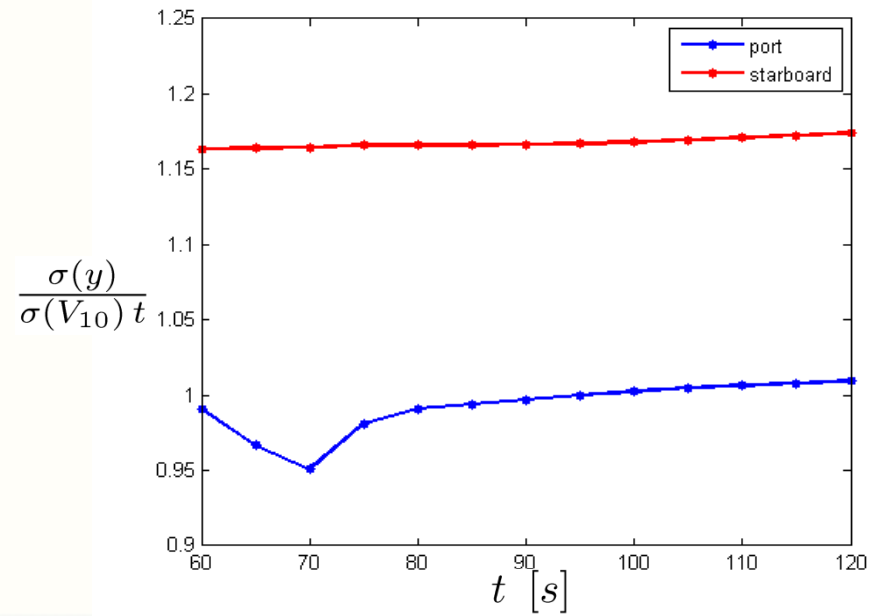
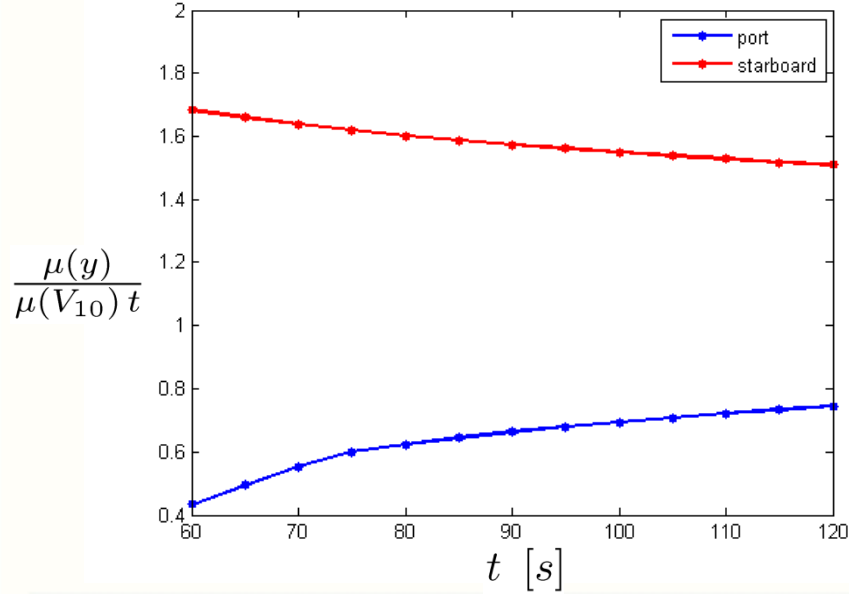


Evolution of normalized mean (left) and standard deviation (right) of the lateral position

• Uniform distribution:

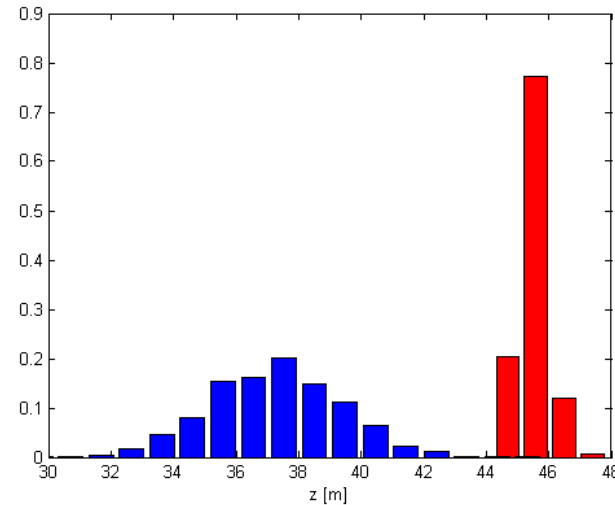
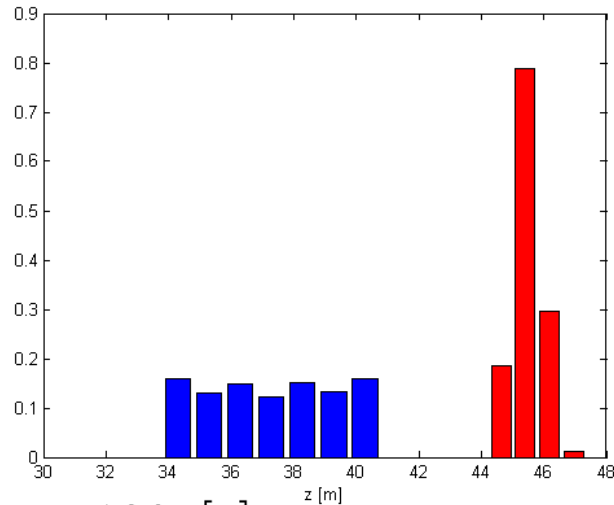


• Normal distribution:



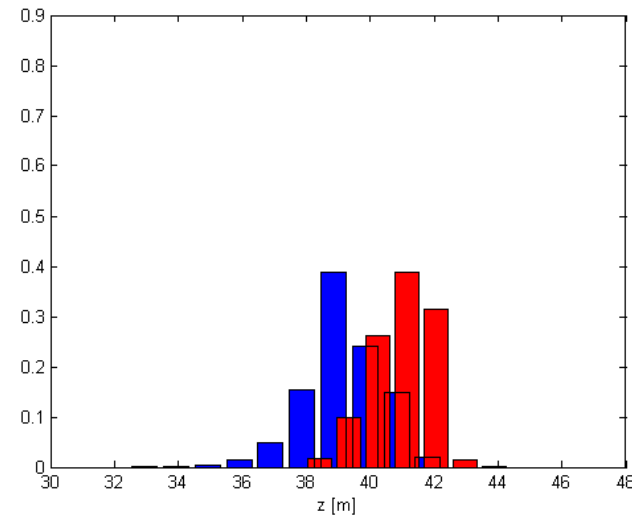
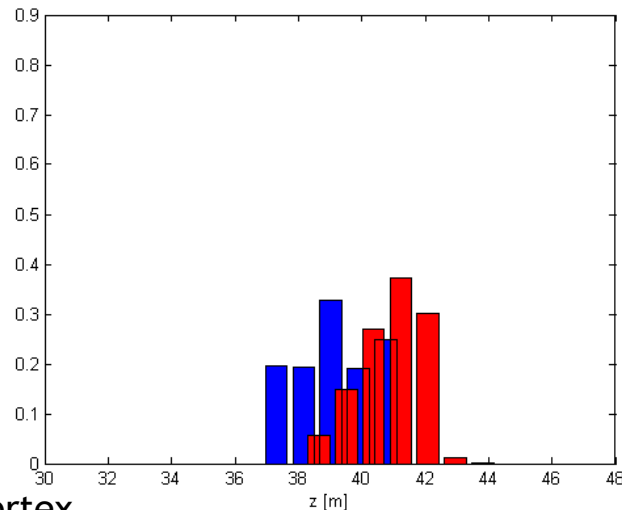
Effect on the altitude position of the vortices

- After $t = 60$ [s] (left/right : uniform/normal distribution of V_{10}) :



Bin size =
1m

- After $t = 120$ [s] :

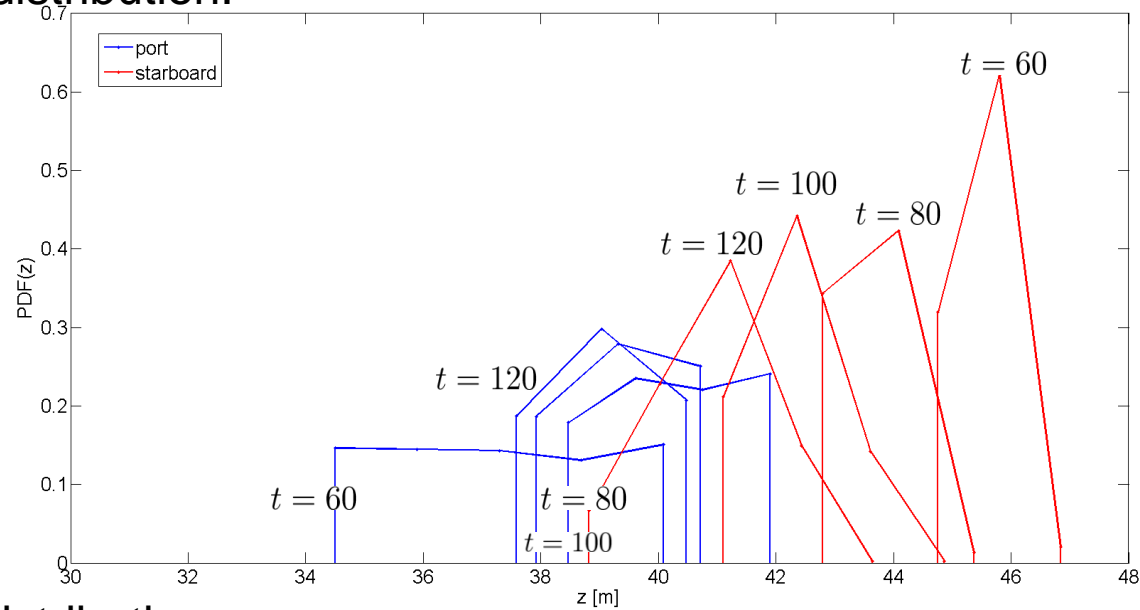


Blue: port vortex

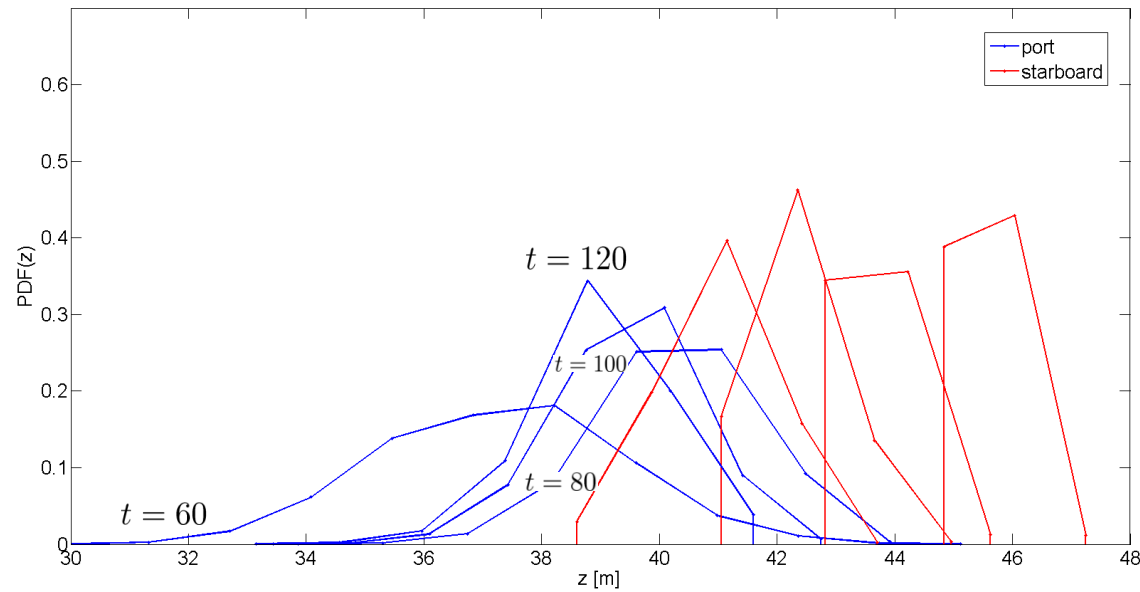
Red: starboard vortex

Evolution of the altitude position discrete PDF

- Uniform distribution:

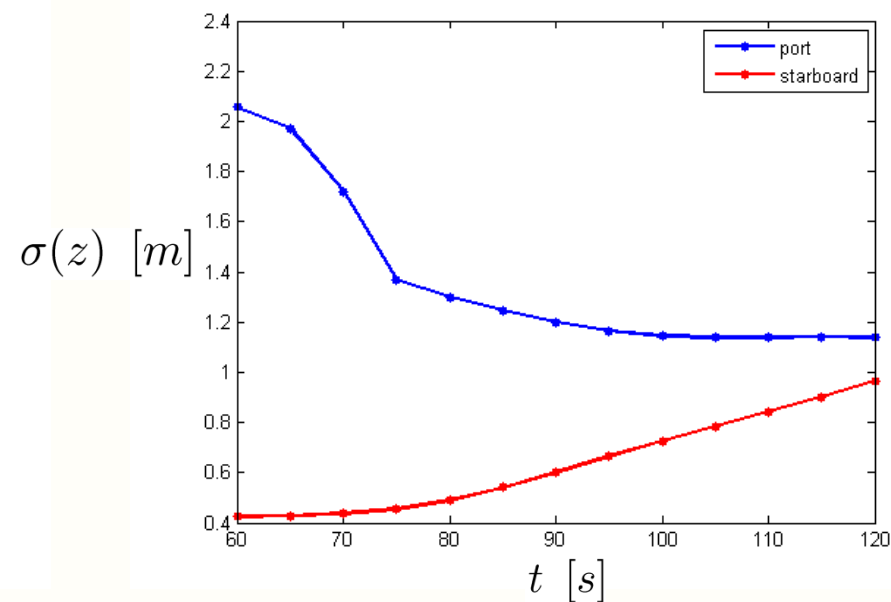
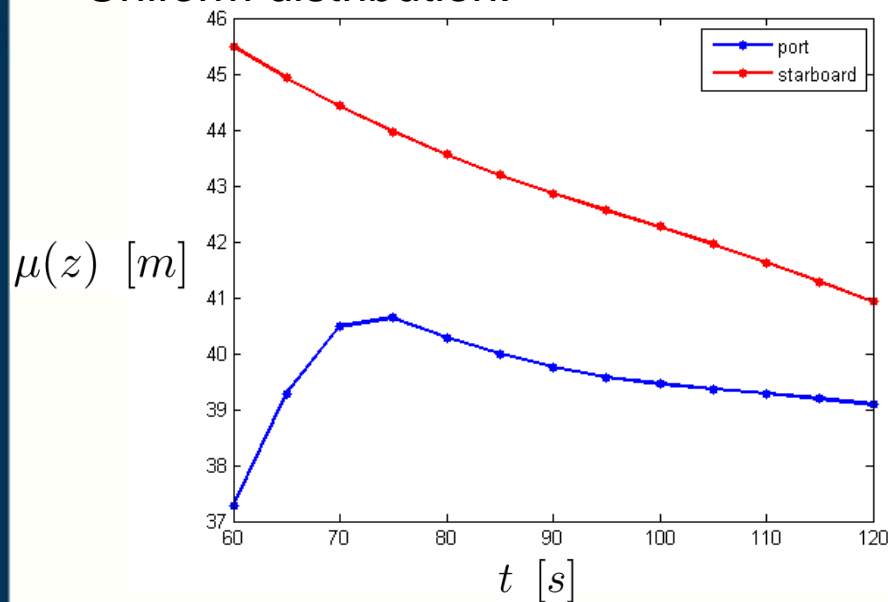


- Normal distribution:

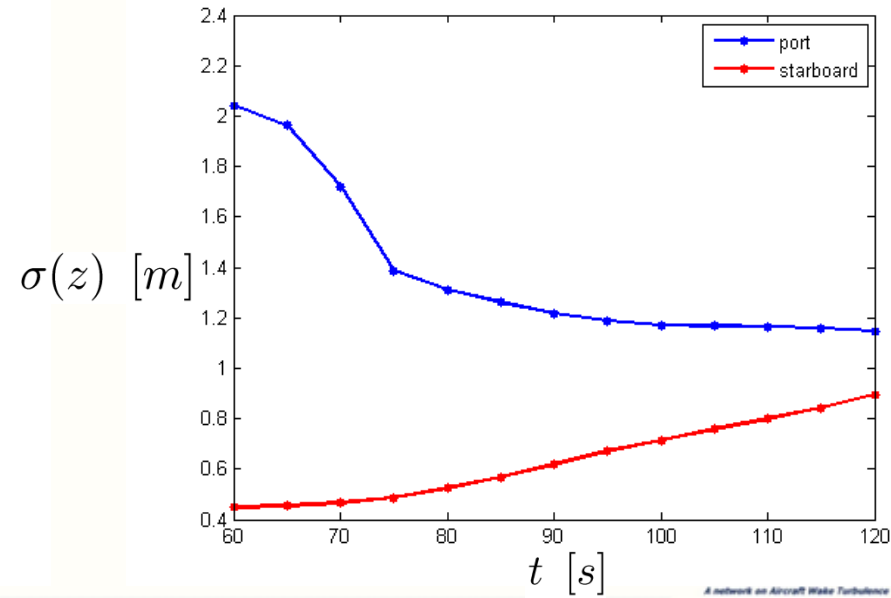
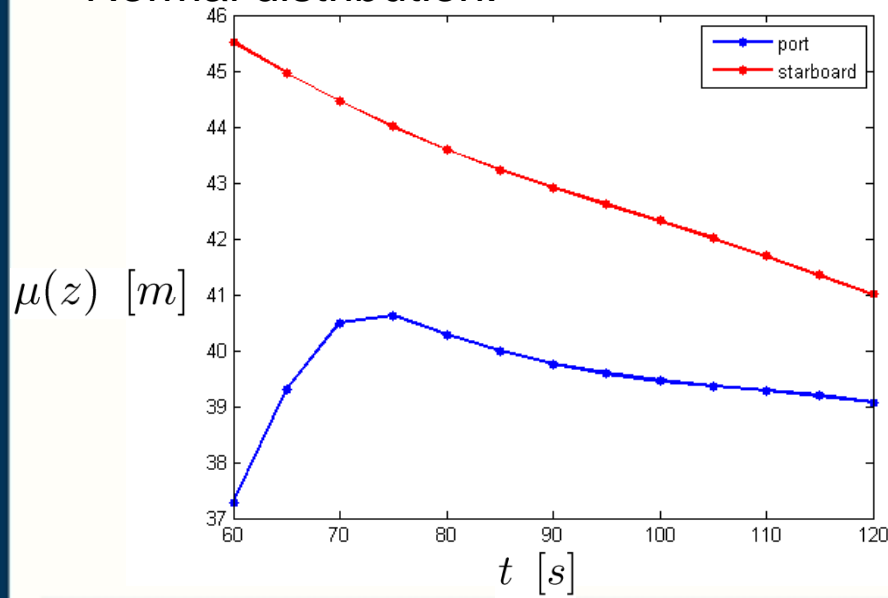


Evolution of mean (left) and standard deviation (right) of the altitude position

- Uniform distribution:

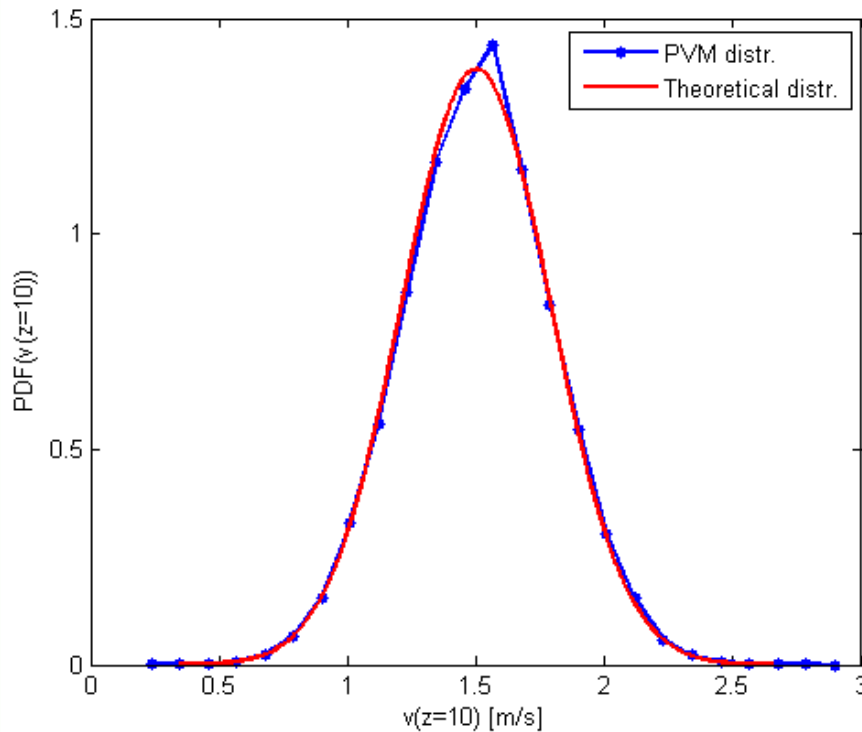


- Normal distribution:



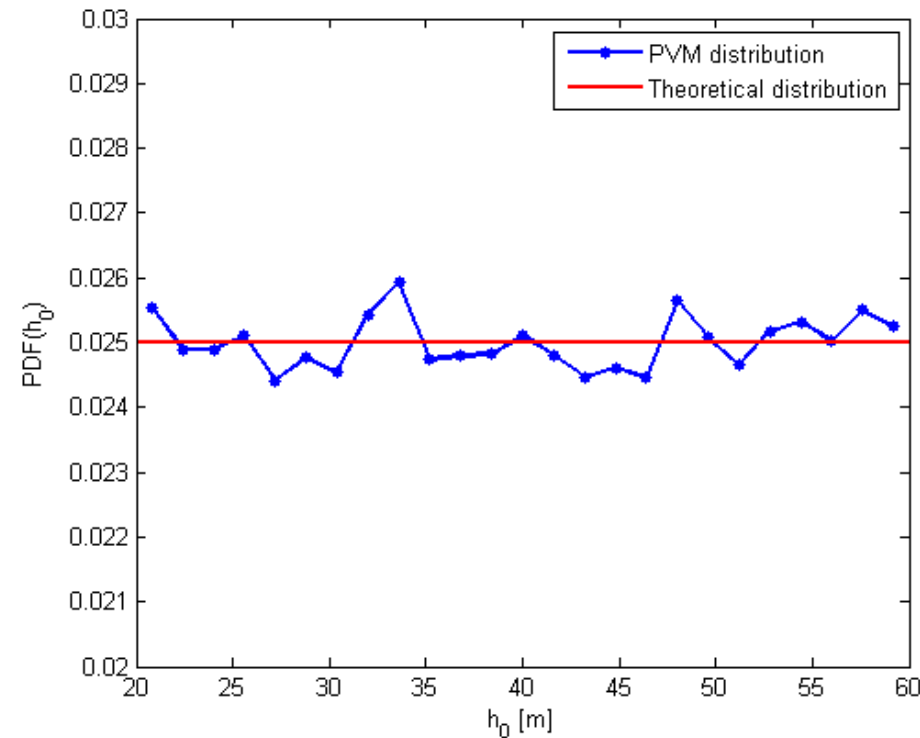
(2) Influences of both V_{10} [m/s] and h_0 [m] distributions

- One investigated case: V_{10} normal (left) and h_0 uniform (right)



$$\mu(V_{10}) = 1.50 \text{ [m/s]}$$

$$\sigma(V_{10}) = 0.29 \text{ [m/s]}$$

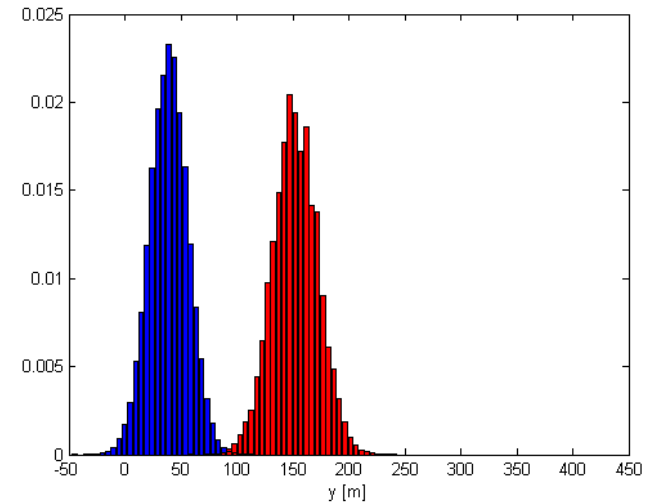
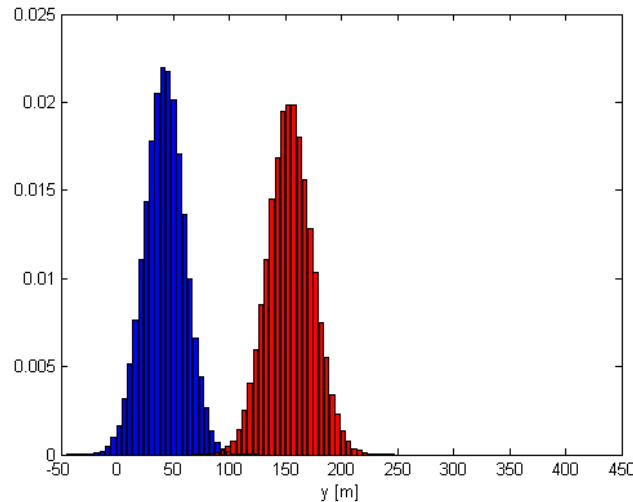


$$h_{0\min} = 20.0 \text{ [m]}$$

$$h_{0\max} = 60.0 \text{ [m]}$$

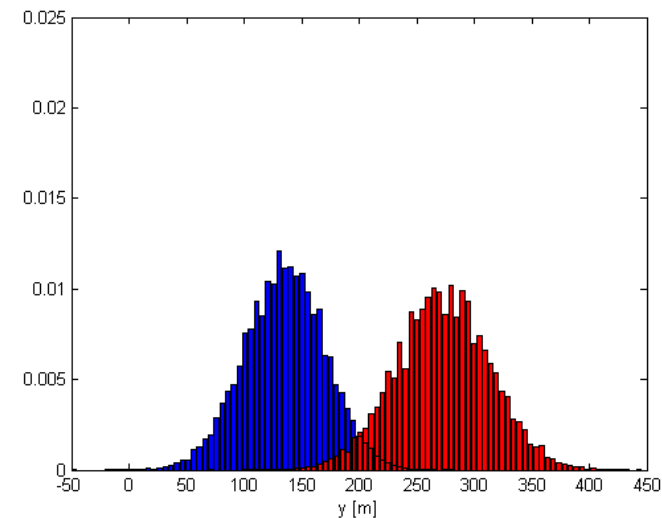
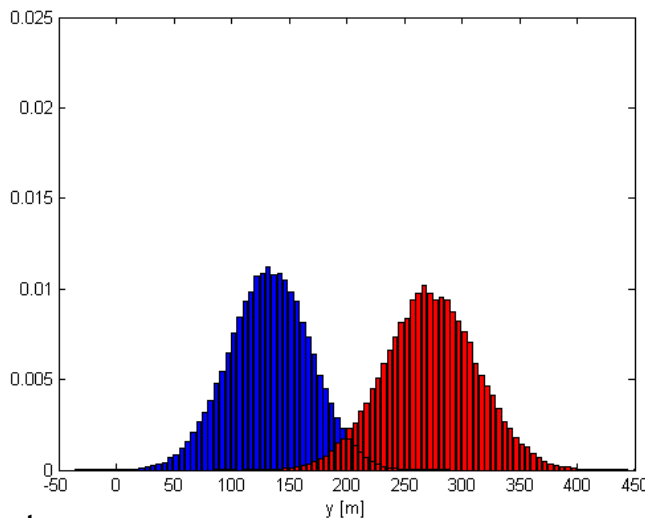
Effect on the lateral position of the vortices

- After $t = 60$ [s] (left: present case, right: previous case) :



Bin size =
5m

- After $t = 120$ [s] :

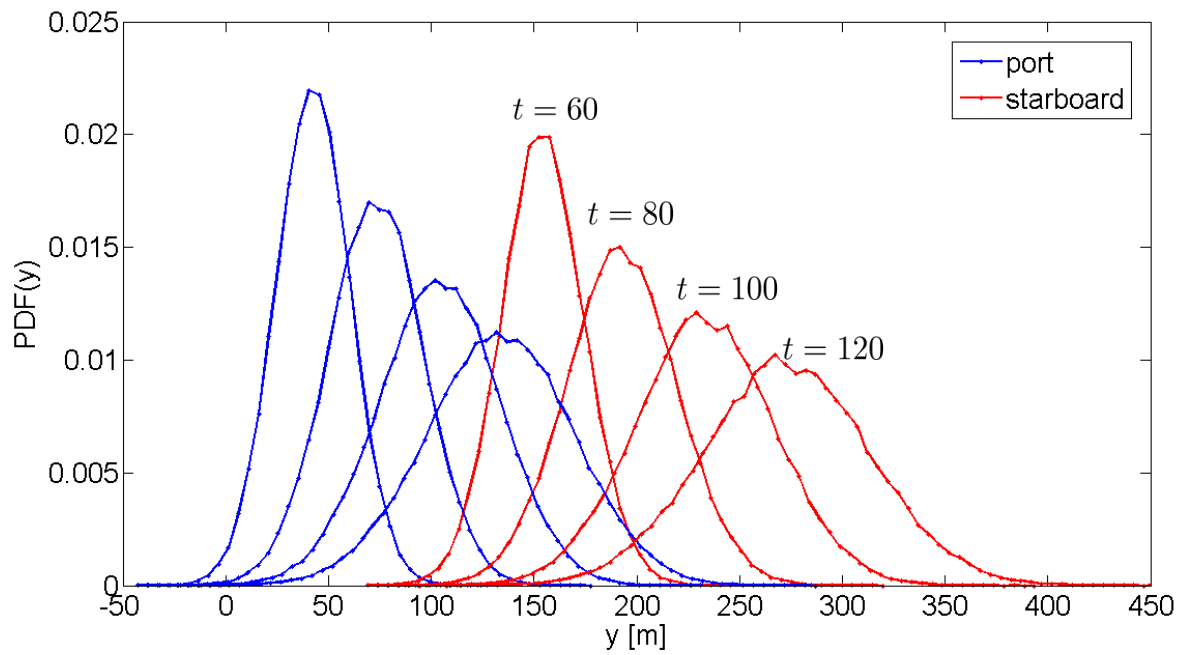


Blue: port vortex

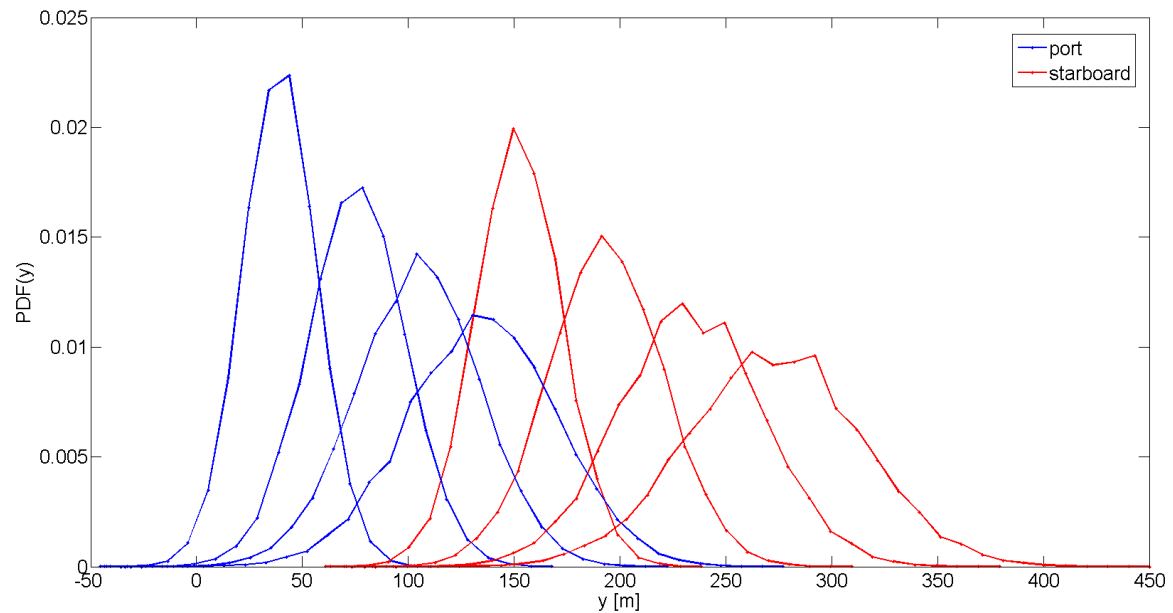
Red: starboard vortex

Evolution of the lateral position discrete PDF

- present case:

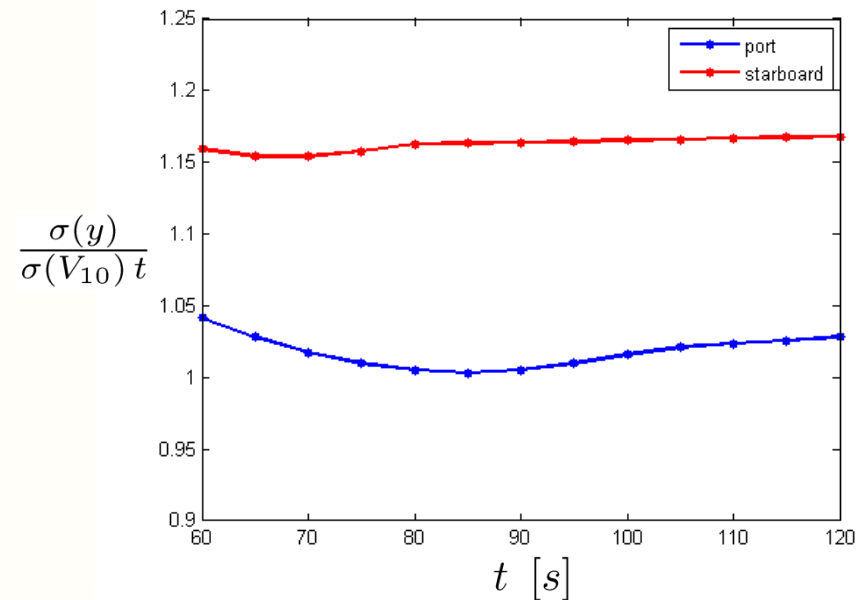
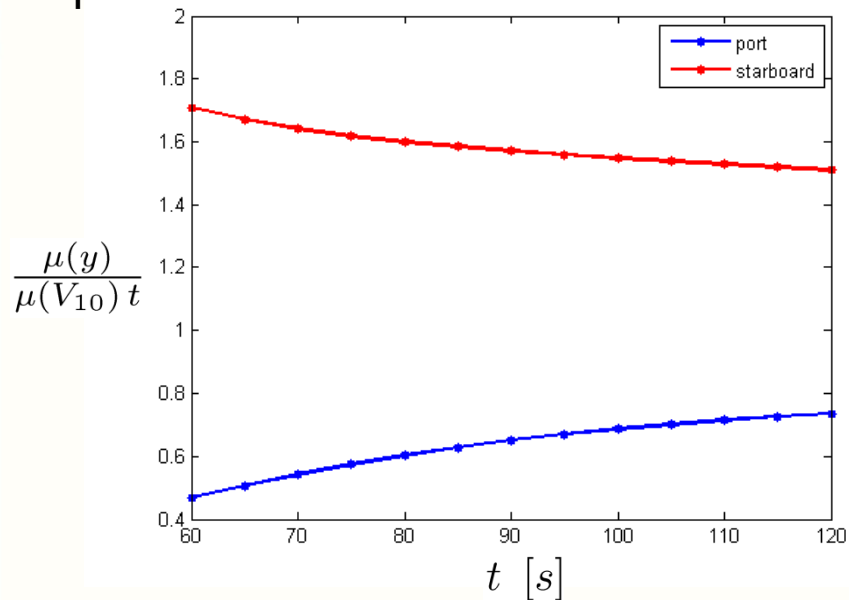


- previous case:

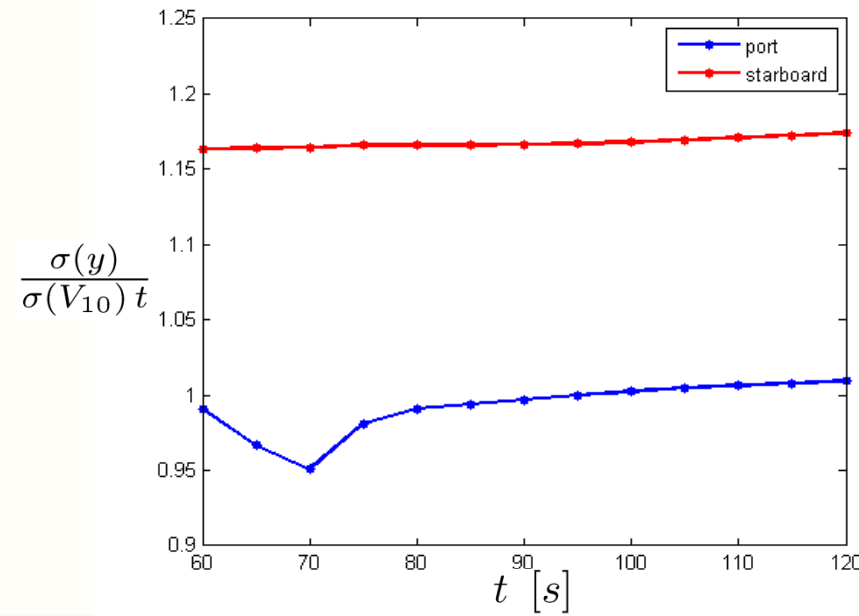
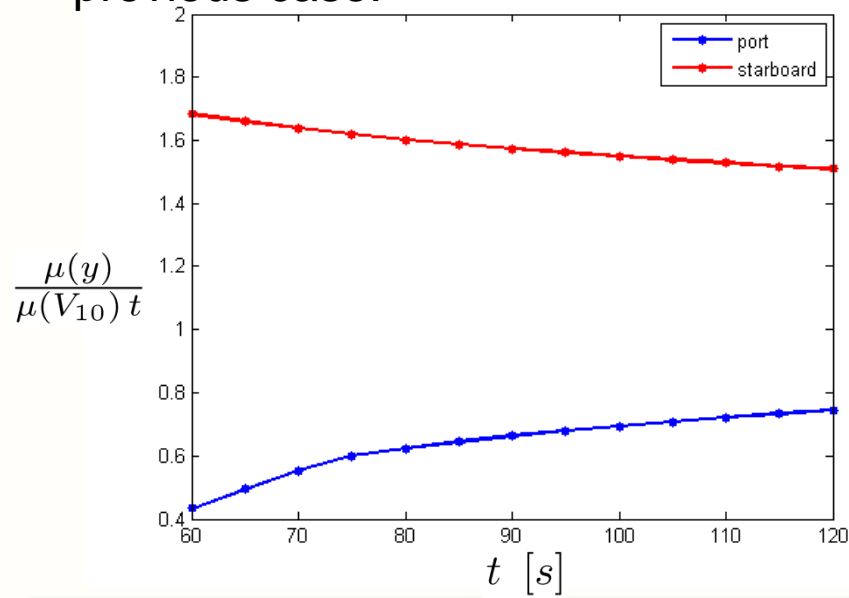


Evolution of normalized mean (left) and standard deviation (right) of the lateral position

• present case:

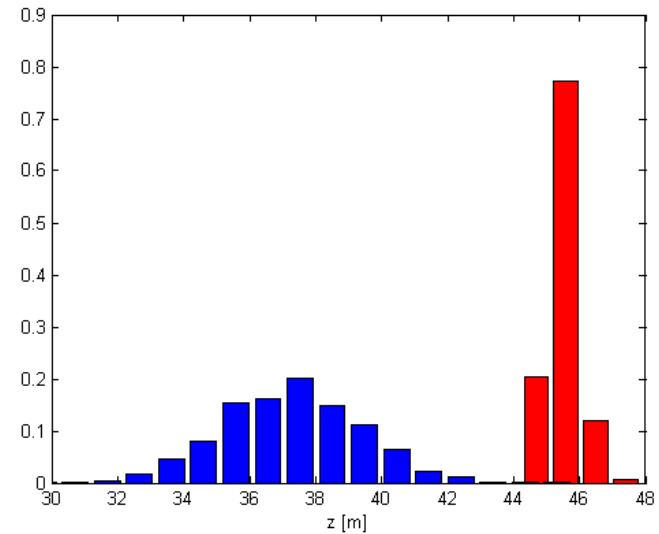
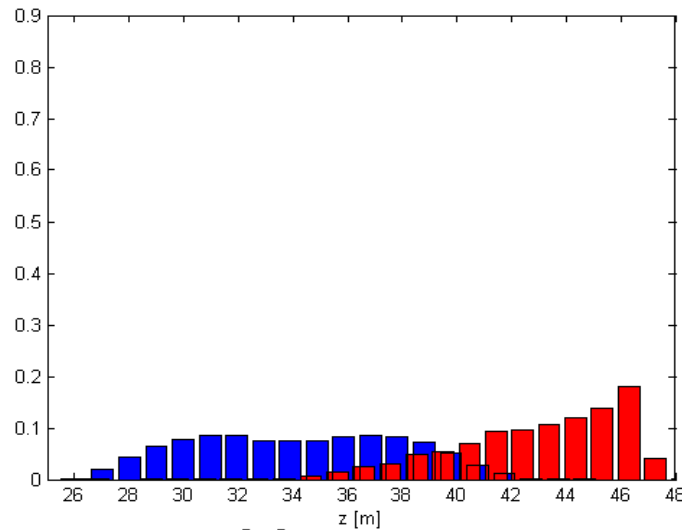


• previous case:



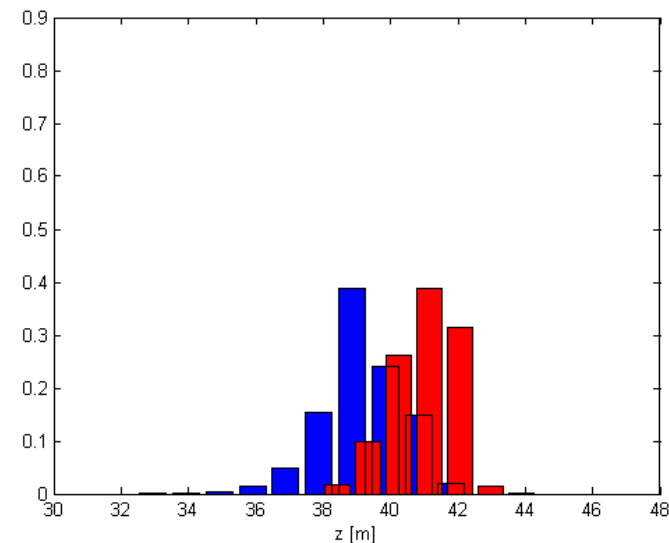
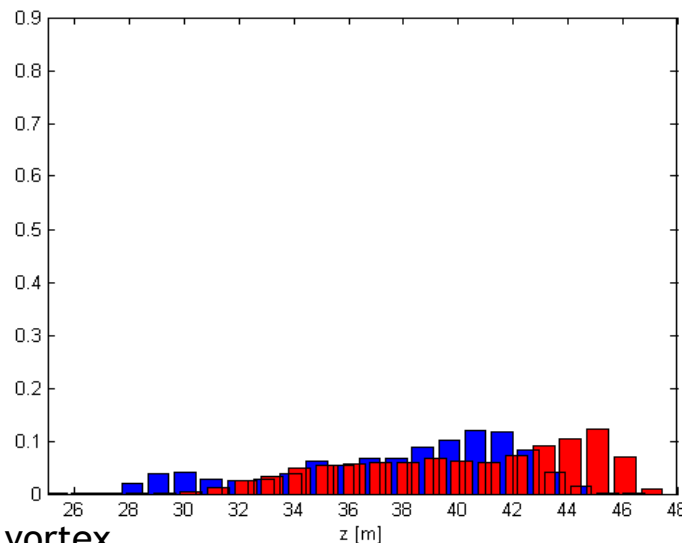
Effect on the altitude position of the vortices

- After $t = 60$ [s] (left: present case, right: previous case) :



Bin size =
1m

- After $t = 120$ [s] :

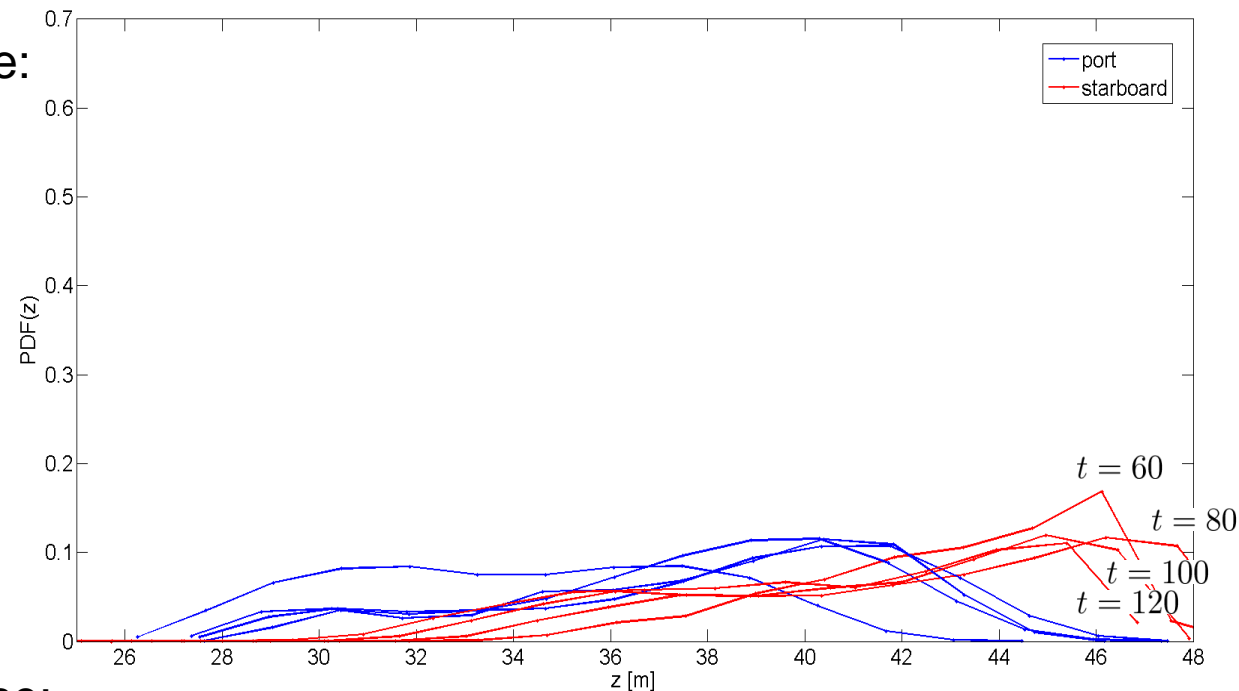


Blue: port vortex

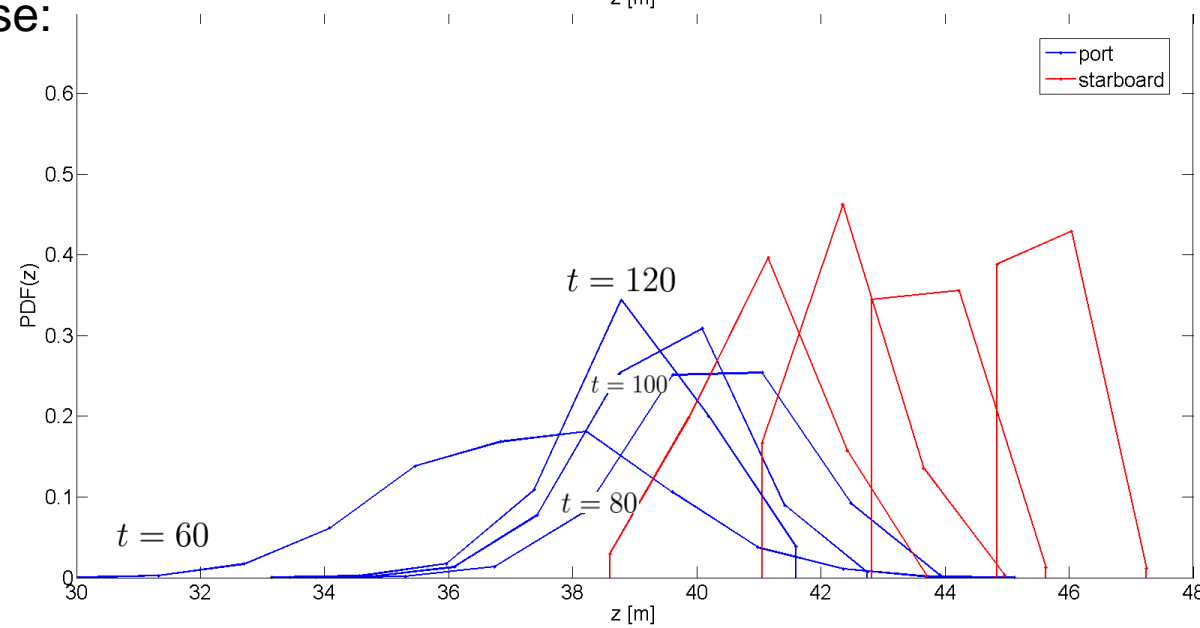
Red: starboard vortex

Evolution of the altitude position discrete PDF

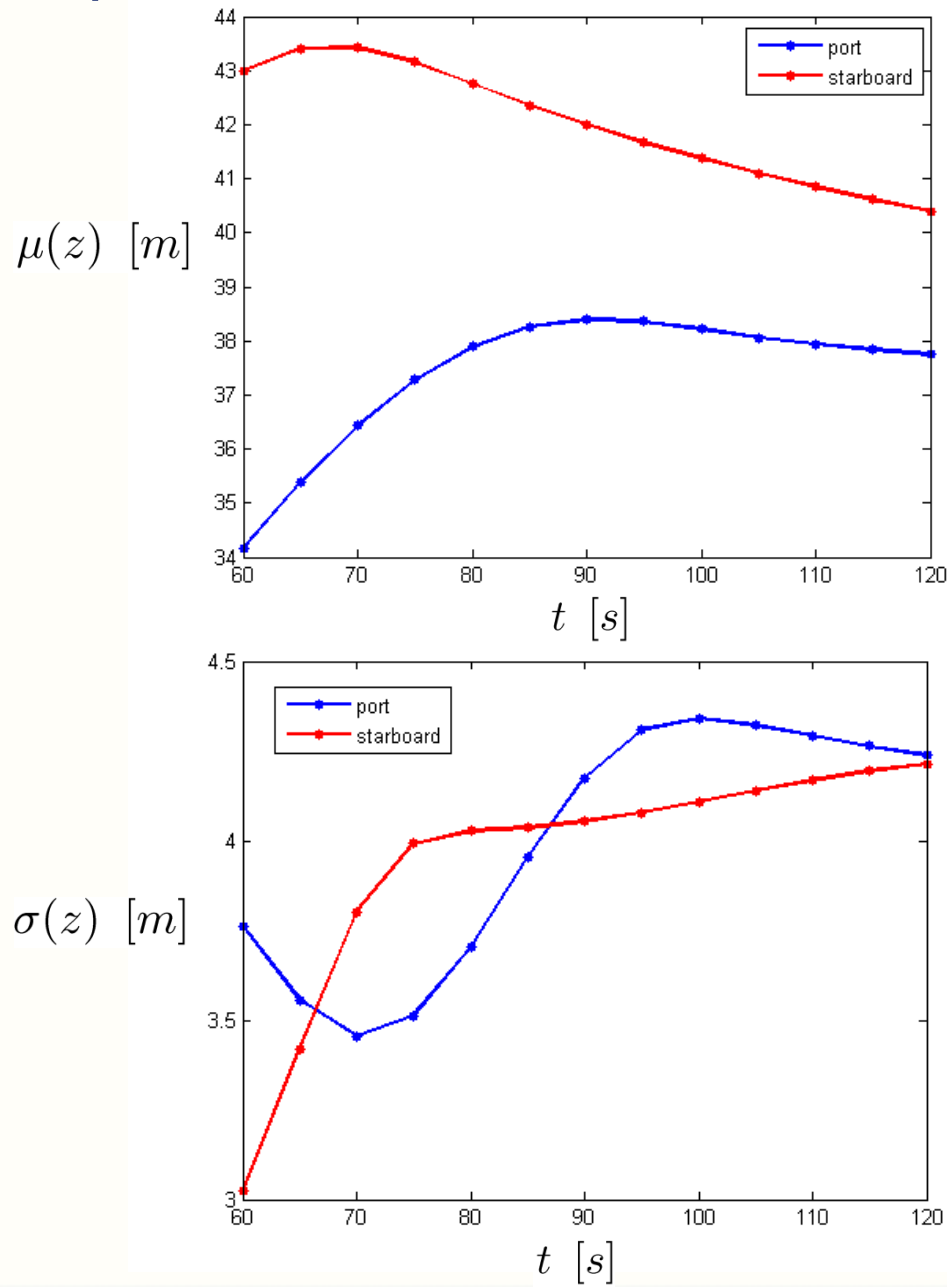
- present case:



- previous case:



Evolution of mean (top) and standard deviation (bottom) of the altitude position



(3) Influence of the distribution of wind orientation α

- Headwind component:

$$\vec{u}_{loc} = V \sin(\alpha) \vec{e}_x$$

- Crosswind component:

$$\vec{v}_{loc} = V \cos(\alpha) \vec{e}_y$$

- Uniform distribution: 3 investigated cases

(i) $\Delta\alpha = \pi/2$

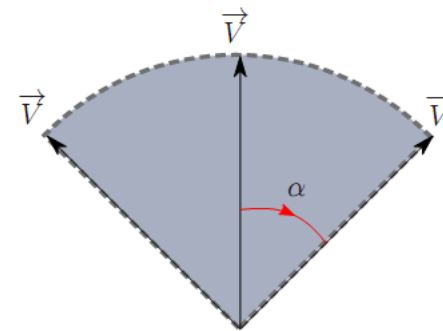
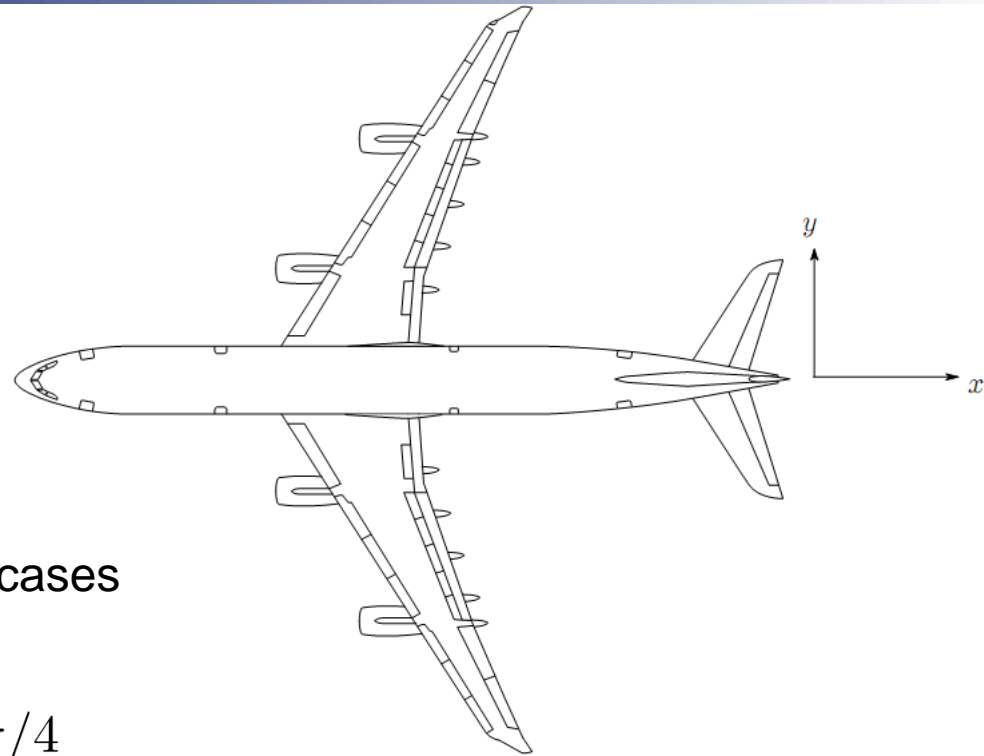
$$\alpha_{\min} = -\pi/4, \alpha_{\max} = \pi/4$$

(ii) $\Delta\alpha = \pi/4$

$$\alpha_{\min} = -\pi/8, \alpha_{\max} = \pi/8$$

(iii) $\Delta\alpha = \pi/6$

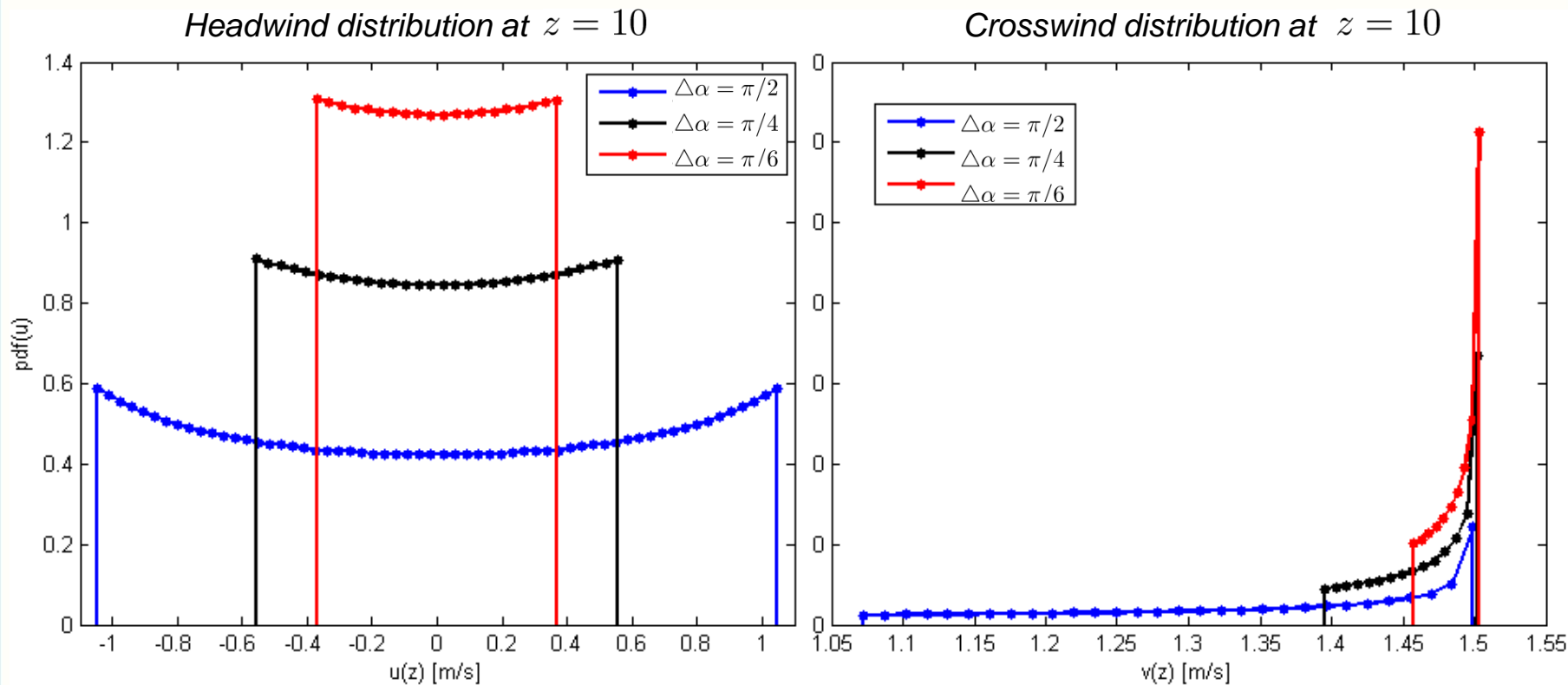
$$\alpha_{\min} = -\pi/12, \alpha_{\max} = \pi/12$$



$$\vec{V} = \vec{u}_{loc} + \vec{v}_{loc}$$

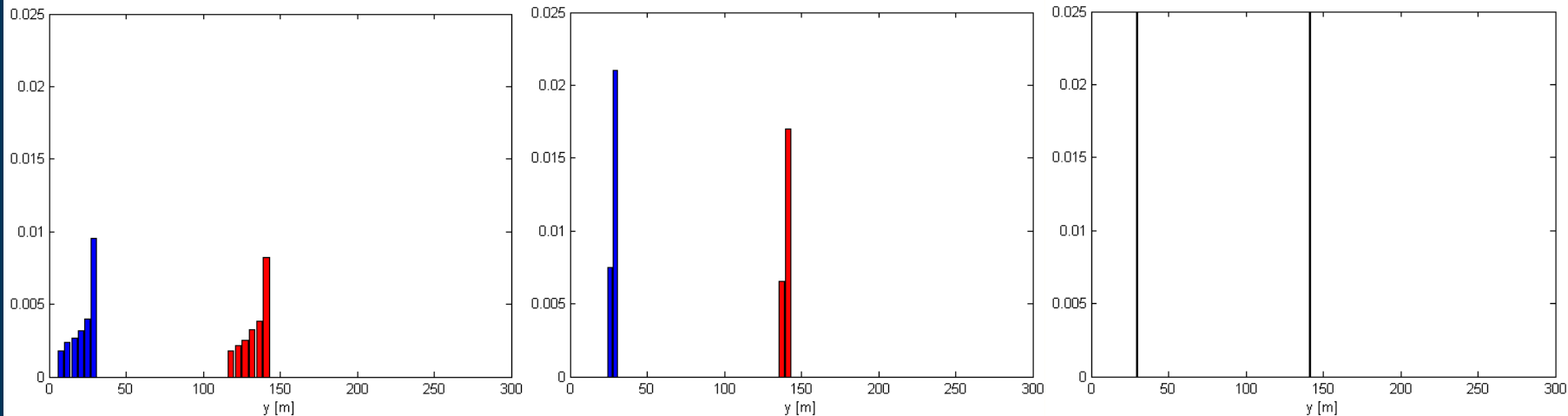
(3) Influence of the distribution of wind orientation α

- Everything else is deterministic
- PVM simulations: 10 000 runs for each of the 3 cases
- Discrete inputs PDF of head- and crosswind:

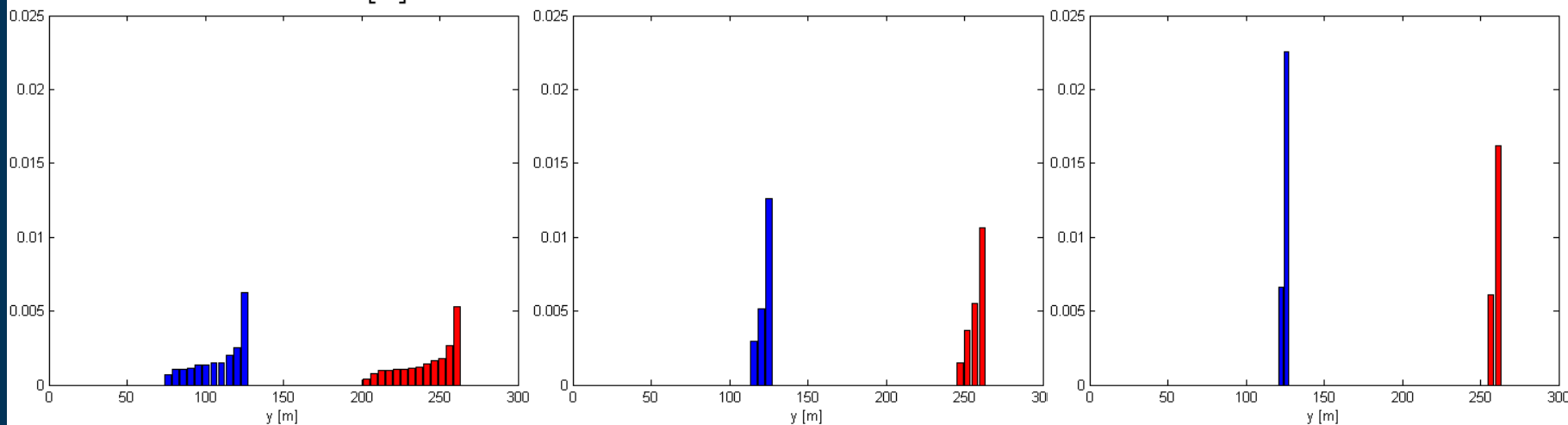


Effect on the lateral position of the vortices

- After $t = 60$ [s] (left: $\Delta\alpha = \pi/2$, middle: $\Delta\alpha = \pi/4$, right: $\Delta\alpha = \pi/6$) :



- After $t = 120$ [s] :



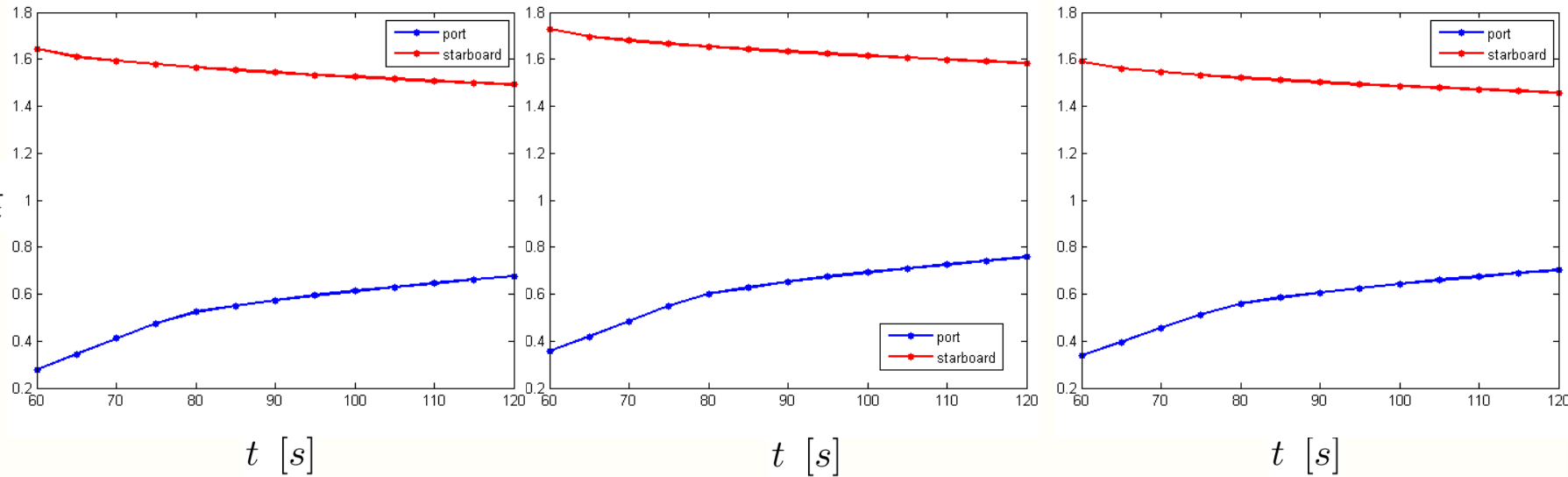
Blue: port vortex

Red: starboard vortex

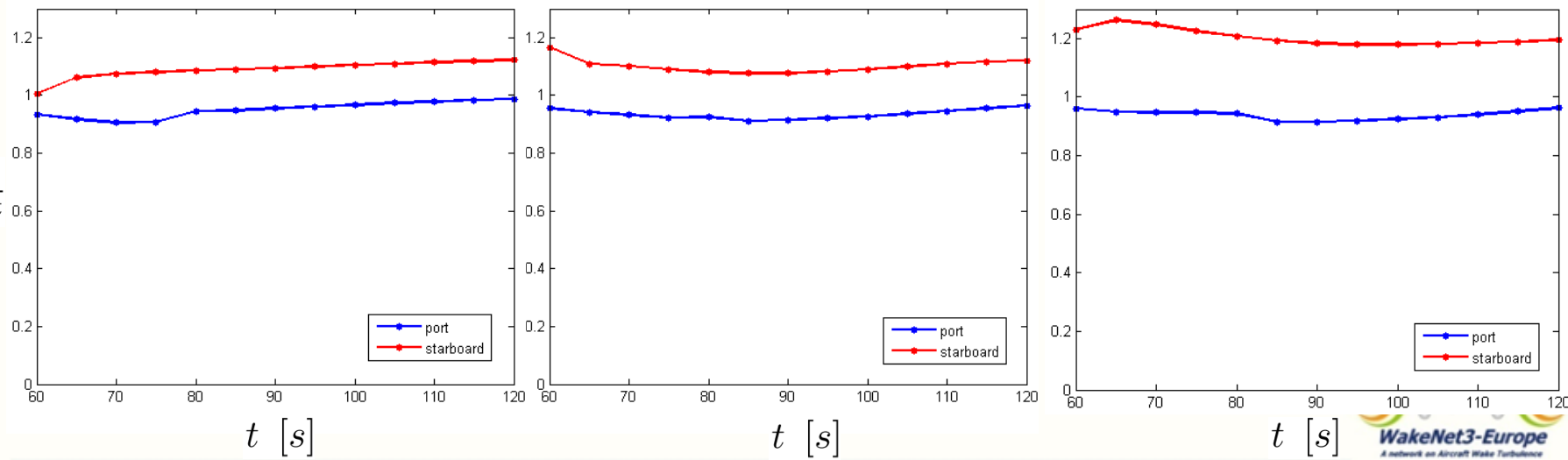
Evolution of normalized mean (top) and standard deviation (bottom) of the lateral position

(left: $\Delta\alpha = \pi/2$, middle: $\Delta\alpha = \pi/4$, right: $\Delta\alpha = \pi/6$) :

$$\frac{\mu(y)}{\mu(V_{10}) t}$$

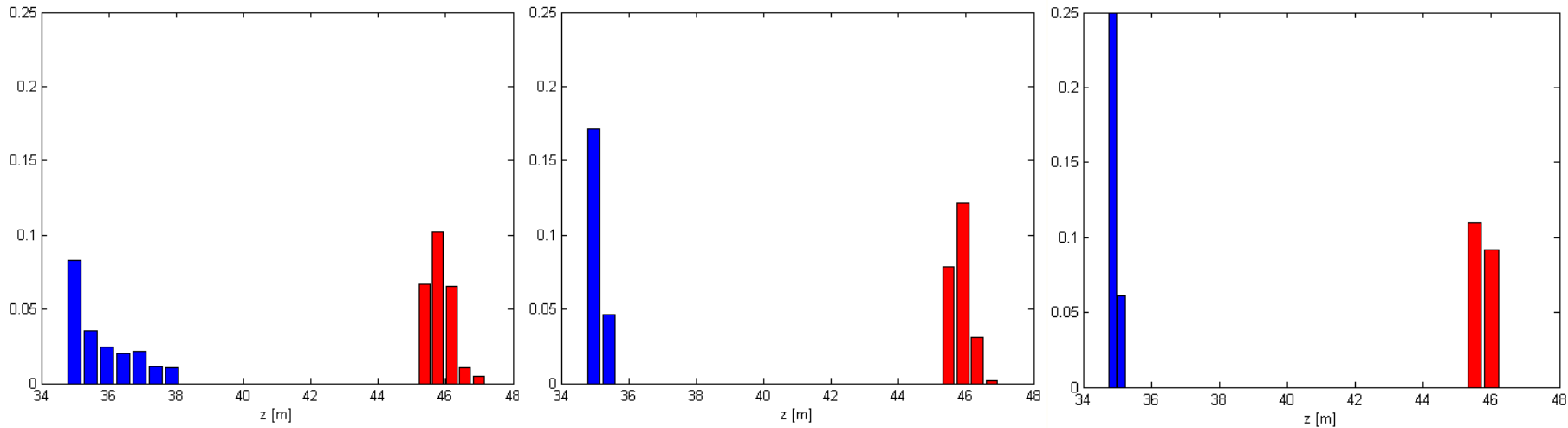


$$\frac{\sigma(y)}{\sigma(V_{10}) t}$$

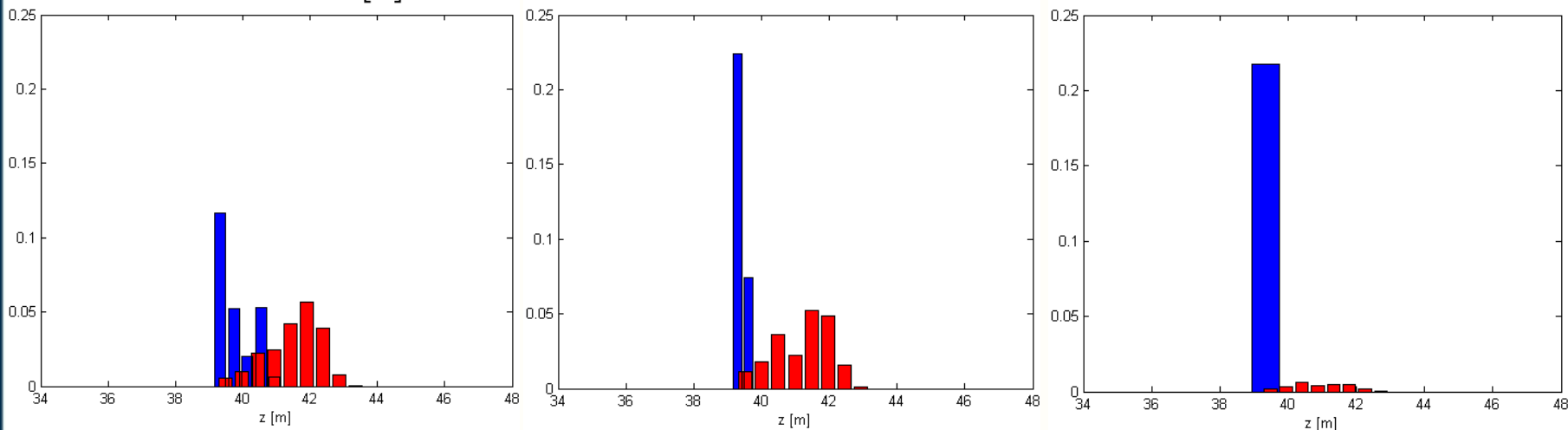


Effect on the altitude position of the vortices

- After $t = 60$ [s] (left: $\Delta\alpha = \pi/2$, middle: $\Delta\alpha = \pi/4$, right: $\Delta\alpha = \pi/6$) :



- After $t = 120$ [s] :



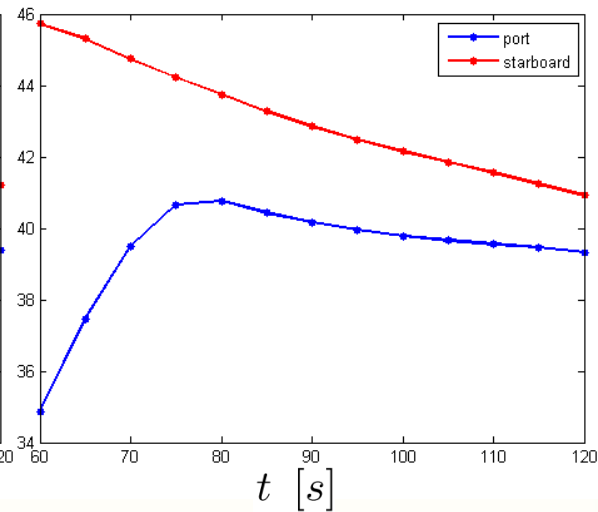
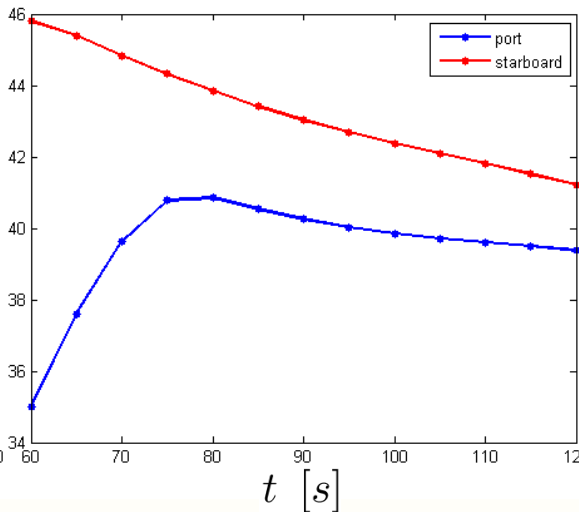
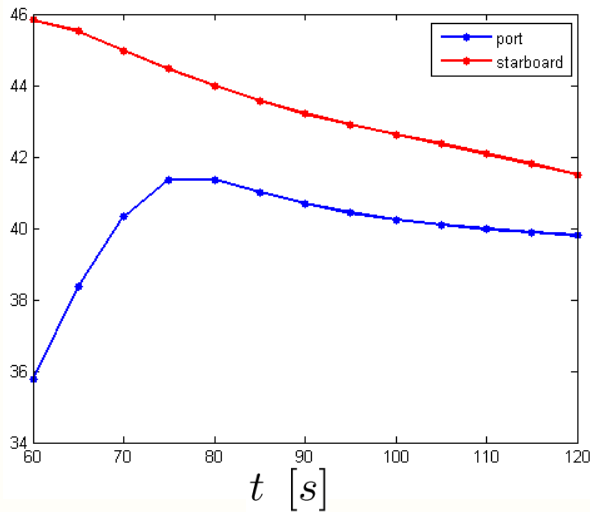
Blue: port vortex

Red: starboard vortex

Evolution of mean (top) and standard deviation (bottom) of the altitude position

(left: $\Delta\alpha = \pi/2$, middle: $\Delta\alpha = \pi/4$, right: $\Delta\alpha = \pi/6$) :

$\mu(z)$ [m]



$\sigma(z)$ [m]

